

Electromagnetically induced transparency in systems with degenerate autoionizing levels in Λ -configuration

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February 22, 2013

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Abstract

We discuss a Λ -like model of atomic levels involving two autoionizing (AI) states of the same energy. The system is irradiated by two external electromagnetic fields (strong – driving and weak – probing ones). For such a system containing degenerate AI levels we derive the analytical formula describing the medium susceptibility. We show that the presence of the second AI level lead to the additional electromagnetically induced transparency (EIT) window appearance. We show that the characteristic of this window can be manipulated by changes of the parameters describing the interactions of AI levels with other ones. This is a new mechanism which leads to additional transparency windows in EIT model, that differs from the mechanism, where a bigger number of Zeeman sublevels is taken into account.

1 Introduction

Electromagnetically induced transparency (EIT) discovered for the first time by Harris and co-workers [1, 2, 3] relies on the destructive quantum interference of the transition amplitudes. Such interference leads to suppression of absorption or even to complete transmission of the resonant weak probe beam. This phenomenon arises in the presence of a second (strong) laser beam coupling coherently one of the states which participate in absorption, with some other atomic state. Some reviews concerning EIT are given in literature (see for instance [4, 5] *and the references quoted therein*). EIT, in its classical model, can be observed for three basic atomic levels configurations. They are Λ -, V -type and cascade (ladder) ones. In these basic schemes, a single peak of enhanced transmission, or one transparency window appears. Nevertheless, one can find in the literature schemes in which additional transparency windows can appear. Such models can be potentially applied for slowing down of light pulses at various frequencies [6]. The models allowing for multiple transparency windows generation were proposed and discussed, for example in [7] (for the cascade system) and in [8, 9] (Λ -model) (*and the references quoted therein*).

EIT phenomena can be discussed not only for the models involving discrete levels but also for those containing continuum ones. In particular, as it was shown in [10, 11, 12], it is possible to create transparency windows for systems with autoionizing (AI) states, or equivalently, with Fano structured continua. Quite recently, in [13] the model with a single AI level was discussed in this context, and the strictly deterministic control laser field was replaced by so-called *white noise* signal.

AI systems involving discrete levels located above a continuum threshold (AI levels) were considered for the first time in the classical paper by Fano [14]. Fano diagonalization, based on the Coulomb mixing of AI states with the continuum, leads to a nontrivial structure of the latter [15, 16, 17] (*and the references quoted therein*). Such structure can be even more complicated, leading to non-trivial effects in the photoelectron spectra, if we assume that the AI system interacts with other ones, not necessarily

containing AI states [18, 19]. Such models can lead to the quantum entanglement generation, as well [20]. It should be stressed out that the models involving structured continuum (or continua) described by the Fano profiles play an essential role in various physical processes, and have also a considerable practical meaning. Since first discussions concerning Fano models in atomic physics [14], the Fano profile has been found in several functioned materials as plasmonic nanoparticles, quantum dots, photonic crystals and electromagnetic metamaterials – for exemplary considerations concerning these problems see [21, 22] *and the references quoted therein*. Discussions concerning those special properties associated with its asymmetric lineshape give us potential applications in a wide range of technologies [23]. An interesting review on Fano profiles in nanostructures is given in [24].

In this paper, we present a model comprising continuum states in which interference between two autoionization channels lead to the appearance of additional transparency EIT windows. The mechanism presented here differs from that for the systems involving only discrete levels without continua. In particular, we shall show that the presence of additional AI states can lead to new quantum interference effects. As a result, the additional EIT windows appear. Moreover, changing the parameters corresponding to the transition to (from) AI states, one can manipulate the characteristic of these windows and the distances between them. However, one should keep in mind that for some particular experimental realizations of our model, some difficulties could appear during adjustment of the parameters involved in the problem.

The model discussed here is an extension of that involving AI resonances considered by Raczyński *et. al* [12] by including the second AI level into our considerations. As it was shown in [25, 26, 27, 28] the presence of additional AI states can lead to new quantum interference phenomena present in the system. As a result, additional zeros can appear in long-time photoelectron spectra. In this paper, for simplicity, we shall restrict ourselves to the case when two AI levels are of the same energy, *i.e.* are degenerate. We shall show that such interference related to the presence of additional AI level can lead to the additional EIT window appearance. Moreover, changing the

parameters corresponding to the transition to (from) AI states, we can manipulate the characteristic of that window. Our model is easily expendable just by adding more than one extra AI state. For such a situation new, supplementary transparency windows will appear.

2 The model and solution

In this Section, we extend the Λ -like model discussed by Raczyński *et.al.* [12] which contains a single autoionizing level and a flat continuum coupled to other two lower discrete ones by an external laser field. In our model, instead of the one AI level we discuss two AI levels $|a_1\rangle$, $|a_2\rangle$ with the same energy $E_1 = E_2$. Moreover, they are embedded in a same flat continuum $|E\rangle$. All of these states are coupled by a weak probe field of frequency ω_p with a discrete level $|b\rangle$ and by a relatively strong driving control field with frequency ω_c with another level $|c\rangle$. The scheme of the model is shown in Fig.1. The configurational coupling between the AI levels $|a_1\rangle$, $|a_2\rangle$ and flat continuum $|E\rangle$ is described correspondingly by the parameters U_1 and U_2 . We call such scheme as a *double- Λ* system.

In the scheme presented here, the coupling between the excited levels $|a_i\rangle$ ($i = \{1, 2\}$) and the lower discrete ones ($|b\rangle$ and $|c\rangle$) is implemented by external laser fields. In particular, the state $|b\rangle$ is coupled to the continuum $|E\rangle$ and AI levels by a weak probe field with amplitude ε_1 , whereas the state $|c\rangle$ by a control field of amplitude ε_2 . It is well-known that non-resonant interactions with other levels leads to level shift. Therefore, the field frequencies (especially, the frequency of the strong driving field ω_2) should be properly chosen for omitting such shift.

We start from the full Hamiltonian for the system

$$\hat{H}' = \hat{H}'_0 + \hat{H}'_1 \quad (1)$$

where

$$\hat{H}'_0 = \sum_{k=1,2} \hbar\omega_{a_k}|a_k\rangle\langle a_k| + \hbar\omega_b|b\rangle\langle b| + \hbar\omega_c|c\rangle\langle c| + \int dE E|E\rangle\langle E| \quad (2a)$$

$$\begin{aligned} \hat{H}'_1 = & \{ \varepsilon_1 \int dE \langle E|d|b\rangle e^{i\omega_p t}|E\rangle\langle b| + \varepsilon_2 \int dE \langle E|d|c\rangle e^{i\omega_c t}|E\rangle\langle c| \\ & + \int dE \langle E|U_1|a_1\rangle + \int dE \langle E|U_2|a_2\rangle \} + H.c., \end{aligned} \quad (2b)$$

where d corresponds to the electric dipole moment, whereas ε_1 and ε_2 describe strengths of the probe and control fields, respectively. Moreover, the matrix elements $\langle E|U_i|a_i\rangle$ ($i = 1, 2$) describe configuration interaction between AI levels and flat continuum states. As usually in the papers concerning AI, we suppose now that the energies of the AI levels and the laser field frequencies are considerably higher than the energy of the threshold of the continuum. In consequence, we can neglect all threshold effects and in consequence, all integrals over the energies, appearing here will be extended over the entire real axis. Moreover, we assume that all matrix elements appearing in (2) and corresponding to the transitions to (from) the flat continuum are energy independent.

It is possible to replace the subset of flat continuum states $\{|E\rangle\}$ and coupled to them AI levels $|a_i\rangle$ ($i = 1, 2$) by continuum states $|E\rangle$ (denoted here by symbols with round brace, contrary to the flat ones labeled by the usually used symbols $|E\rangle$) with some structure (density function). This function can be derived with use of *Fano diagonalization* method proposed in [14] and then developed, for instance in [17]). This procedure leads to the scheme in which discrete levels $|b\rangle$ and $|c\rangle$ are coupled to the excited continuum characterized by some density of states. This density function is referred as to *double Fano profile*. Its shape is determined by the ratio between the matrix elements corresponding to the transitions from (to) a some considered discrete level $|j\rangle$ to (from) a flat and structured continua [14, 25]:

$$\frac{\langle j|d|E\rangle}{\langle j|d|E\rangle} = \frac{(E - E_1)(E - E_2) + E(q_{1j}\gamma_1 + q_{2j}\gamma_2) - (E_1q_{2j}\gamma_2 + E_2q_{1j}\gamma_1)}{(E - E_1)(E - E_2) - iE(\gamma_1 + \gamma_2) + i(E_1\gamma_2 + E_2\gamma_1)}, \quad (3)$$

where the widths $\gamma_1 = \pi|\langle a_1|U_1|E\rangle|^2$ and $\gamma_2 = \pi|\langle a_2|U_2|E\rangle|^2$ are autoionization widths of AI states. Similarly as in [25], we defined *Fano asymmetry parameters* q_{1j} and q_{2j}

which can be expressed as:

$$q_{1j} = \frac{\langle j|d|a_1\rangle}{\pi\langle j|d|E\rangle\langle E|U|a_1\rangle} \quad , \quad (4a)$$

$$q_{2j} = \frac{\langle j|d|a_2\rangle}{\pi\langle j|d|E\rangle\langle E|U|a_2\rangle} \quad , \quad (4b)$$

where $j = b, c$. These parameters describe ratios between the direct transition between one of the lower states and AI state and its counterpart via (flat) continuum state. It follows from the form of (4) that when the direct ionization is negligible, the values of the q -parameters become high.

After performing the diagonalization procedure, the system can be described by following Hamiltonian:

$$\hat{H}'' = \hat{H}_0'' + \hat{H}_1'' \quad (5)$$

where

$$\hat{H}_0'' = \hbar\omega_b|b\rangle\langle b| + \hbar\omega_c|c\rangle\langle c| + \int dE E|E\rangle\langle E| \quad (6a)$$

$$\hat{H}_1'' = \{\varepsilon_1 \int dE (E|d|b\rangle e^{i\omega_p t}|E\rangle\langle b| + \varepsilon_2 \int dE (E|d|c\rangle e^{i\omega_c t}|E\rangle\langle c|)\} + H.c. \quad (6b)$$

In this formula, all excited levels considered here are replaced by structured continuum states $|E\rangle$.

For further study, we derive the appropriate equations for the density matrix ρ . For this purpose, we use Liouville-von Neumann equation and apply the *rotating wave approximation* (RWA) [29] which allows to remove rapidly rotating terms from our set of equations. This procedure leads to the following differential equations for the matrix elements of the density matrix ρ :

$$i \hbar \dot{\rho}_{Eb} = (E - E_b - \hbar\omega_p) \rho_{Eb} - \frac{1}{2}\varepsilon_1 (E|d|b\rangle - \frac{1}{2}\varepsilon_2 (E|d|c\rangle) \rho_{cb} \quad (7a)$$

$$i \hbar \dot{\rho}_{cb} = (E + \hbar\omega_c - E_b - \hbar\omega_p - i\hbar\gamma_{cb}) \rho_{cb} - \frac{1}{2}\varepsilon_2^* \int \langle c|d|E\rangle \rho_{Eb} dE \quad , \quad (7b)$$

where the Fano diagonalization formalism was applied. The above equations are valid within the first order perturbation with respect to the probe field ε_1 . The parameter d appearing here is the electric atomic dipole moment and the matrix elements $\rho_{Eb} =$

$(E|\rho|b\rangle$ and $\rho_{Ec} = (E|\rho|c\rangle$. Moreover, similarly as in [12], we have introduced the width γ_{cb} . It is a phenomenological relaxation rate for the coherence ρ_{cb} .

In general, it is possible to find the full solution of the differential equations (7), but we shall restrict our considerations to the long-time limit and find the steady-state solution following the way described in [12]. To solve eqns. (7), first we eliminate ρ_{cb} expressing it in terms of ρ_{Eb} to get the integral equation which will be solved in the next step, and next, ρ_{Eb} will be found.

Since, we are interested in EIT, we should calculate the component of the electric polarization of the irradiated medium. It can be expressed as a function of the matrix element ρ_{Eb} in the following way

$$\begin{aligned} P^+(\omega_p) &= N \int \langle b|d|E\rangle \rho_{Eb} dE \\ &= -N\varepsilon_1 \left(R_{bb} + \frac{\frac{1}{4}\varepsilon_2^2 R_{bc}R_{cb}}{E_b + \hbar\omega_p - E_c - \hbar\omega_c - i\hbar\gamma_{cb} - \frac{1}{4}\varepsilon_2^2 R_{cc}} \right) = \epsilon_0 \varepsilon_1 \chi(\omega_p) \end{aligned} \quad (8)$$

where N is the atom density, ϵ_0 is the vacuum electric permittivity, whereas χ is the medium susceptibility. In our model, the last can be expressed as [12]

$$\chi(\omega_p) = -\frac{N}{\epsilon_0} \left(R_{bb} + \frac{\frac{1}{4}\varepsilon_2^2 R_{bc}R_{cb}}{E_b + \hbar\omega_p - E_c - \hbar\omega_c - i\hbar\gamma_{cb} - \frac{1}{4}\varepsilon_2^2 R_{cc}} \right) \quad (9)$$

with

$$R_{jk}(\omega_p) = \lim_{\substack{\eta \rightarrow 0^+ \\ \Delta E \rightarrow 0^+}} \int \frac{\langle j|d|E\rangle \langle E|d|k\rangle}{E_b - E + \hbar\omega_p + i\eta} dE \quad , \quad (j, k = b, c) \quad . \quad (10)$$

The limit $\eta \rightarrow 0^+$ assures that the imaginary part of χ will be greater than zero, whereas $\Delta E = E_2 - E_1$ tends to zero for the degenerate AI levels. It is worth noting that the function inside the integral contains matrix elements corresponding to the transitions to (from) the structured continuum $|E\rangle$. Since such elements are energy dependent, we apply the formula (3) to get the explicit dependence of the integrand on the energy. Thus, we can write

$$R_{jk}(\omega_p) = \lim_{\substack{\eta \rightarrow 0^+ \\ \Delta E \rightarrow 0^+}} D_j D_k \int \frac{F_j(E) F_k(E)}{E_b - E + \hbar\omega_1 + i\eta} dE \quad , \quad j, k = b, c \quad , \quad (11)$$

where the functions $F_j(E), F_k(E)$ inside the integral correspond to matrix elements related to the transitions to (from) the structured continuum $|E\rangle$. The matrix elements

of the dipole moment transition $\langle j|d|E\rangle$ and $\langle E|d|k\rangle$ are denoted by D_j and D_k , respectively. As it was emphasized earlier, we neglect threshold effects, so we extend the integration limits for $R_{jk}(\omega_p)$ from minus to plus infinity. Thanks to this assumption (and other mentioned earlier), we can find the analytical solution for this parameter and hence, for the medium susceptibility χ .

3 Results and discussion

Since we deal with the degenerate case the analytical solution for $R_{jk}(\omega_p)$ can be written as:

$$R_{jk} = D_j D_k (Q_j + i)(Q_k - i) \pi \left\{ \frac{-i}{(Q_j + i)(Q_k - i)} - \frac{2i\Gamma}{(Q_j + i)(\omega + i\Gamma)} - \frac{2i\Gamma^2}{\omega^2 + \Gamma^2} + \frac{\Gamma}{\omega - i\Gamma} + \frac{\Gamma[Q_{j21}Q_{k21} + \Gamma_{21}^2 Q_j Q_k + \Gamma_{21}(Q_{j21}Q_k + Q_{k21}Q_j)]}{(1 - \Gamma_{21}^2)(Q_j Q_k - i(Q_j - Q_k) + 1)\omega} \right\} \quad (12)$$

where the argument was redefined as $\omega = \hbar\omega_p + E_b - E_1$. Similarly as in [25], we introduced here the effective asymmetry parameters $Q_j, Q_{j21}, \Gamma_{21}$ and AI width Γ defined as

$$Q_j = \frac{q_{1j}\gamma_1 + q_{2j}\gamma_2}{\Gamma} \quad , \quad j = c, b \quad (13a)$$

$$\Gamma = \gamma_1 + \gamma_2 \quad . \quad (13b)$$

Moreover, we defined the quantities

$$Q_{j21} = \frac{q_{2j}\gamma_2 - q_{1j}\gamma_1}{\Gamma} \quad , \quad j = c, b \quad (13c)$$

$$\Gamma_{21} = \frac{\gamma_2 - \gamma_1}{\Gamma} \quad . \quad (13d)$$

If we assume that the both AI levels are characterized by the same values of parameters describing interaction between them and other levels, *i.e.* asymmetry parameters and AI widths, the quantities $\Gamma_{21} = 0, Q_{b21} = Q_{c21} = 0$. In consequence, our result becomes identical to that derived by Raczyński *et. al* [12].

Further, for easier comparison of our results to those presented in [12] we take the same values for the parameters describing our system as those presented there. Thus, we assume that $\Gamma = 10^{-9}$ a.u., $D_b = 2$ a.u., $D_c = 3$ a.u. and the atomic density

$N = 0.33 \times 10^{12} \text{ cm}^{-3}$. Moreover, the values of the asymmetry parameters are assumed to be $\sim 10 \div 100$, whereas the field amplitude ε_2 is within the range from 10^{-9} to 10^{-6} a.u.

Thus, Fig. 2 shows the real (dispersion) and imaginary (absorption) parts of the medium susceptibility as a function of the frequency $\omega = \omega_p + (E_b - E_1)/\hbar$ expressed in the units of Γ . Actually, we see that for the case when $\Gamma_{21} = 0, Q_{b21} = Q_{c21} = 0$ (solid line), we get the same result as that for the model with a single AI level discussed by Raczynski *et.al* [12]. In fact, this is the situation mentioned above, when two degenerate AI levels can be treated as a single one described by the effective asymmetry parameter and AI width. However, if we assume that the parameters describing two AI levels differ each other, *i.e.* $Q_{b21} \neq 0$ and $Q_{c21} \neq 0$, situation changes considerably. For such an additional zero appears in $Im\chi$, leading to the second absorption window occurrence (dashed-dotted line). In consequence, two windows are apparent and they are placed symmetrically with respect to the point $\omega = 0$. The position of these windows depends on the values of the parameters describing our system and for some cases the windows coalesce to a single one with a sharp peak inside (dashed line). Such behavior resembles that discussed in [25], concerning long-time photoelectron spectrum. The second window for our model corresponds to the additional zero in the spectrum discussed in [25] as a result of existence of extra ionization channel via the second AI level. In consequence, an additional quantum interference effect becomes present in the system leading to generation of the second zero in photoelectron spectra and the transparency window, as well. Moreover, for the system considered here one can observe an additional region of anomalous dispersion related to the presence of the second transparency window (as we compare our result with that discussed in [12]). Thus, the presence of the second AI state in the system can lead to nontrivial results, analogously to the situation presented in the discussion concerning photoelectron spectra [25, 26, 27, 28].

The structure of created windows is very clear. It can be manipulated in potential applications, for example in simultaneous slowing down of light pulses at various fre-

quencies [6]. In particular, the position and widths of the transparency windows can be changed by the strength of control field. In Fig. 3 we show the real and imaginary parts of the medium susceptibility again for various strengths of this field intensity ϵ_2 . One can see that its changes can influence the positions and widths of the windows. If we increase the value of ϵ_2 , both the distance between the windows and their widths increases considerably. Thus, we can use the intensity of the control field as a control parameter for EIT effects.

In Figures 4 and 5, we show how the values of the autoionization widths can influence the number, position and width of the transparency windows. Thus, Fig. 4 corresponds to the situation when the effective asymmetry parameters $Q_{b21} = Q_{c21} = 0$. For this case the result resembles that for the model involving single AI level, discussed in [12]. We observe only single transparency window, and its position and width do not depend on the value of Γ_{21} . We can only observe well-defined changes in the amplitude of variations of the real and imaginary parts of χ , so the depth of the window becomes more distinct as Γ_{21} increases. However, if we assume that Q_{b21} and Q_{c21} becomes different from zero (see Fig. 5) situation changes considerably again. Similarly as in Figs. 2 and 3, additional transparency window and region of anomalous dispersion appears again. From Fig. 5 we see that with increasing difference between the values of AI widths (Γ_{21}), the separation and widths of the both windows become more pronounced. These facts justify the statements that the phenomena related to the autoionization processes strongly depend on the continuum shape and their characters. The strengths of the effects observed in the system can be changed considerably by varying the parameters describing the profile of the continuum, so we can have various possibilities of controlling these phenomena in practice.

4 Conclusions

In this paper we considered the Λ -like model involving two AI levels (for simplicity we assumed that they are of the same energy). This model is an extension of that with a single AI level, discussed by Raczyński *et.al* [12]. For such a model we have derived

the analytical formula describing the media susceptibility χ . We have shown that due to the presence of the second AI level we can observe additional transparency window and extra region of the anomalous dispersion. We have shown that the properties (position, and width) of the window depend on the values of the parameters describing the interaction of these levels with the driving field. Moreover, the depth of the window can be manipulated by changes of the asymmetry parameters related to the transitions induced by the probe field and especially depends on the difference between the values of the autoionization widths. In addition, for the degenerate case if the parameters describing two AI levels are identical, our model behaves as that with one AI level characterized by some effective AI width and asymmetry parameter. If the parameters corresponding to the two AI levels start to differ each other, the additional EIT window appears despite the presence of degeneracy. This situation resembles that discussed in [25] concerning the long-time photoelectron spectra, when for various values of the AI level's parameters an additional zero appeared for the degenerate case. This is a result of the existence of two channels of autoionization and quantum interference between them. Such interference disappears if two AI levels are identical. We have shown that inclusion of additional AI state into the model can lead to the new and interesting effects that are absent for single level's models.

The most important phenomenon discussed here is the appearance of the additional transparency windows in the system, where various channels of ionization (autoionization) exist. Such channels can interfere each other giving new EIT windows. These effects could seem to be similar to those observed in the systems involving only discrete levels but they are of completely different physical character. Indeed, for the model discussed here, we deal with a structured continuum interacting with two discrete ground levels. In consequence, for the system considered here, we have a new possibility to simultaneous slowing down of light pulses at various frequencies.

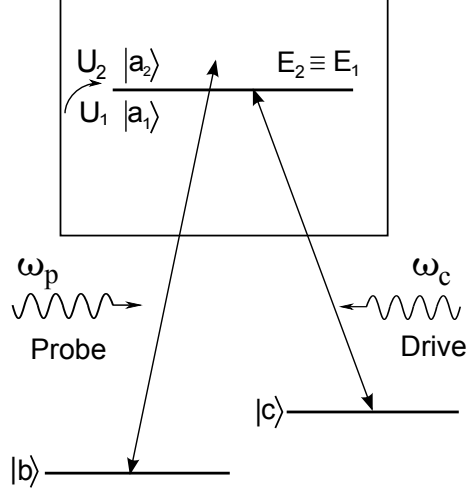


Fig.1 Scheme of the discussed model. Due to presence of the configurational interaction coupling (U_1 and U_2) between the two AI levels $|a_1\rangle$ and $|a_2\rangle$, and the flat continuum $|E\rangle$ all these states can be replaced by the double Fano structured continuum $|E\rangle$. This continuum ($|E\rangle$) is coupled by the weak probe and strong control fields of the frequencies ω_p and ω_c , respectively.

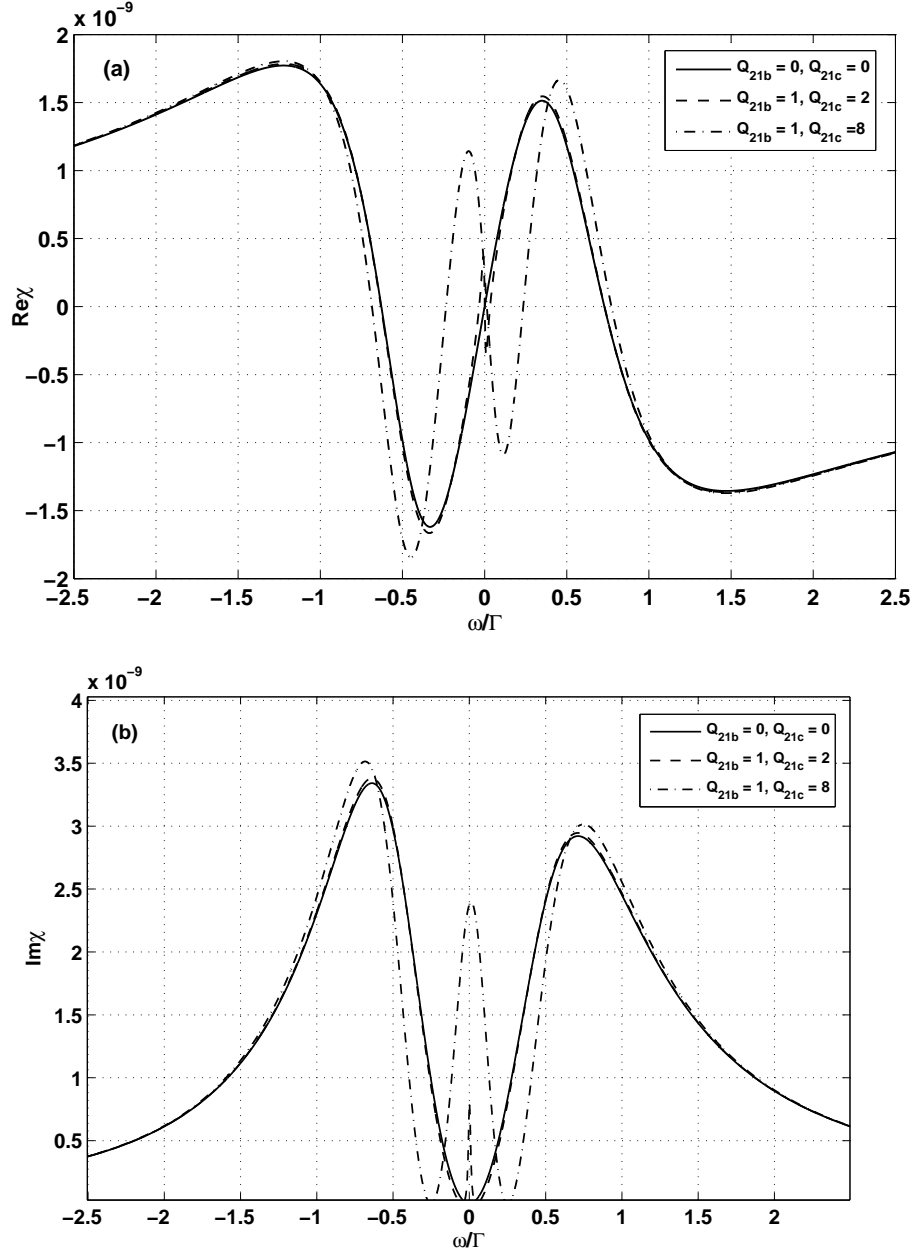


Fig.2 The real (a) and imaginary (b) parts of the susceptibility χ as a function of the detuning ω (in units of Γ). We assume that $\epsilon_2 = 4 \times 10^{-7}$ a.u., $\Gamma_{21} = 0$ and $Q_b = Q_c = 20$. Solid lines – $Q_{b21} = Q_{c21} = 0$, dashed lines – $Q_{b21} = 1, Q_{c21} = 2$, – dashed dotted lines $Q_{b21} = 1, Q_{c21} = 8$.

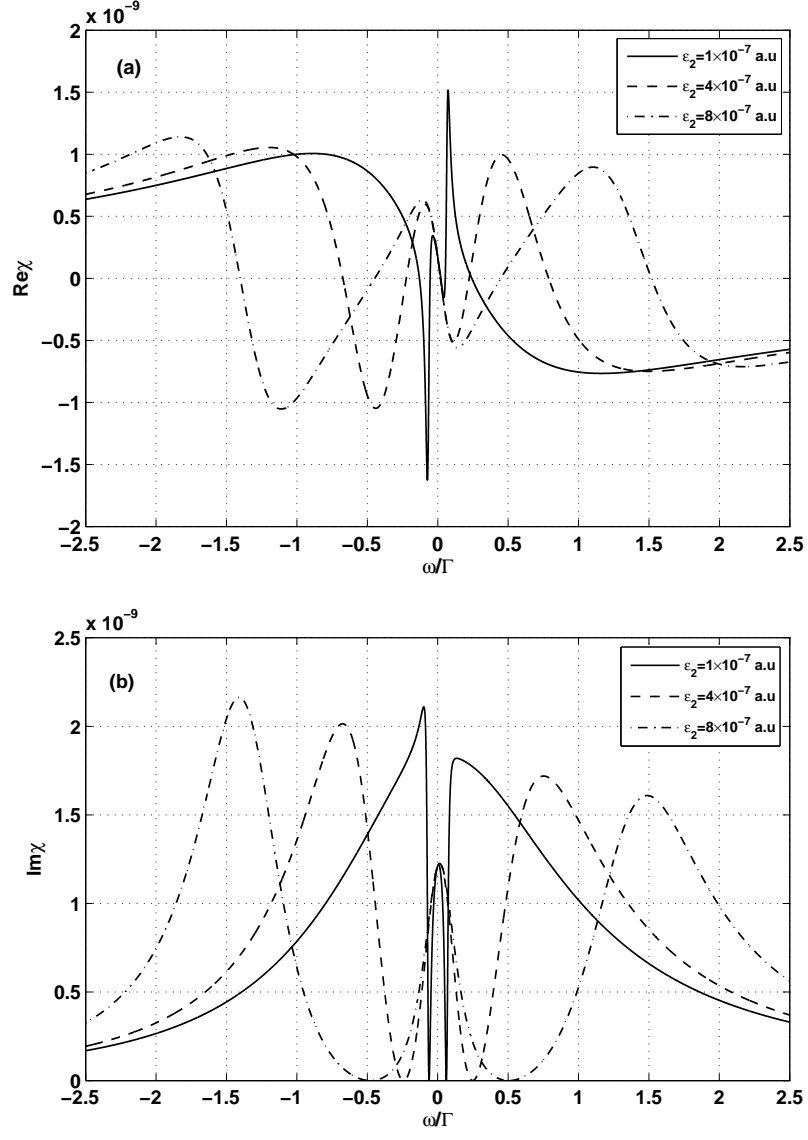


Fig.3. The same as in Fig.2 but for $Q_{b21} = 1, Q_{c21} = 8$ and various values of ϵ_2 . The remaining parameters are the same as in Fig.2.

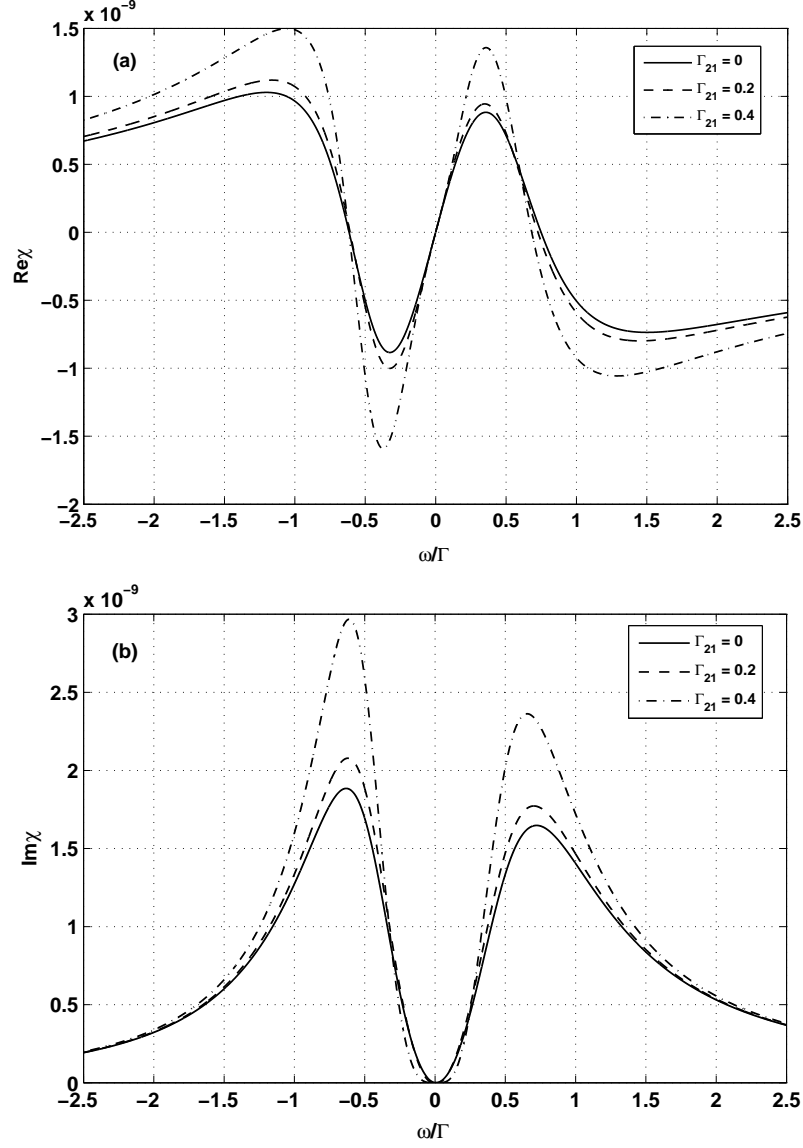


Fig.4. The real (a) and imaginary (b) parts of the susceptibility χ as a function of the detuning ω (in units of Γ) for identical AI levels ($Q_{b21} = Q_{c21} = 0$) and various values of Γ_{21} . We assume that $\epsilon_2 = 4 \times 10^{-7}$ a.u., and $Q_b = 15, Q_c = 20$.

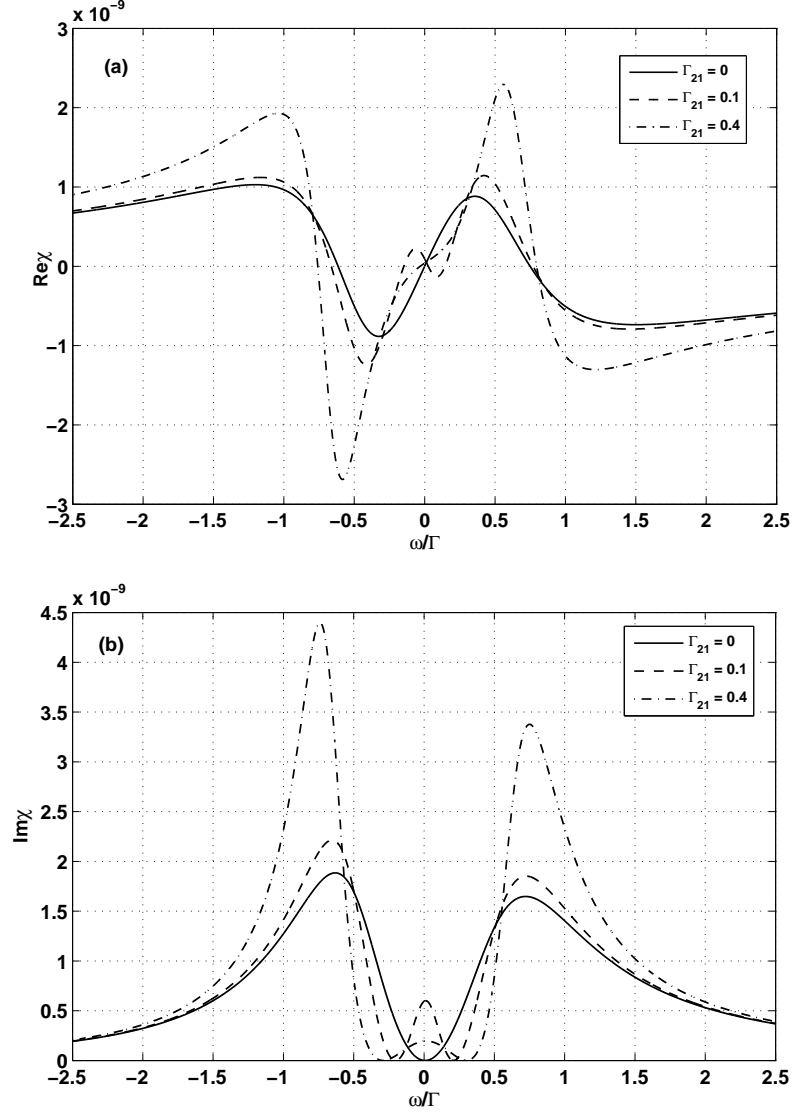


Fig.5. The real (a) and imaginary (b) parts of the susceptibility χ for various values of Γ_{21} , Q_{b21} and Q_{c21} . Solid lines – $Q_{b21} = Q_{c21} = 0, \Gamma_{21} = 0$, dashed lines – $Q_{b21} = 1, Q_{c21} = 6, \Gamma_{21} = 0.1$, – dashed dotted lines $Q_{b21} = 1, Q_{c21} = 6, \Gamma_{21} = 0.4$. The remaining parameters are the same as in Fig.4.

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